Kanren Light
A Dynamically Semi-Certified Interactive Logic Programming System

MARCO MAGGESI, University of Florence, Italy
MASSIMO NOCENTINI, University of Florence, Italy

We present an experimental system strongly inspired by miniKanren, implemented on top of the tactics mechanism of the HOL Light theorem prover. Our tool is at the same time a mechanism for enabling the logic programming style for reasoning and computing in a theorem prover, and a framework for writing logic programs that produce solutions endowed with a formal proof of correctness.

CCS Concepts: • Theory of computation → Interactive computation; Streaming models; Logic and verification; Automated reasoning.

Additional Key Words and Phrases: miniKanren, HOL Light, Certified, Theorem Proving, Program verification

1 INTRODUCTION
In straightforward terms, the computation of a logic program evolves by refining a substitution seeking for solutions of a unification problem. This has been made explicit in the Kanren approach [1, 5, 7], where programs are described by composing (higher-order) operators that act on streams of substitutions. Such a methodology allows for a streamlined approach to logic programming; however, the intended semantics and the correctness of a Kanren program rest entirely on the meta-theoretic level.

We propose a framework that extends the Kanren approach to a system that computes both candidate substitutions and corresponding certificates of correctness with respect to a given specification. Such certificates will be formally verified logical truths synthesized using a theorem prover.

Our setup is based on the HOL Light theorem prover [6], in which we extend the currently available tactic mechanism with three basic features: (i) the explicit use of meta-variables, (ii) the ability to backtrack during the proof search, (iii) a layer of tools and facilities for interfacing with the underlying proof mechanism.

The basic building block of our framework are ML procedures that we call solvers, which are a generalization of HOL tactics and are –as well as tactics– meant to be used compositionally in order to define arbitrarily complex proof search strategies.

We say that our approach is semi-certified because

• on the one hand, the synthesized solutions are formally proved theorems, hence their validity is guaranteed by construction;
• on the other hand, the completeness of the search procedure cannot be enforced in our framework and consequently has to be ensured by a meta-reasoning.

Authors’ addresses: Marco Maggesi, University of Florence, Italy, marco.maggesi@unifi.it; Massimo Nocentini, University of Florence, Italy, massimo.nocentini@unifi.it.

This work is licensed under a Creative Commons “Attribution-NonCommercial-NoDerivatives 4.0 International” license.

© 2020 Copyright held by the author(s).
miniKanren.org/workshop/2021/8-ART5
Moreover, we say that our system is dynamically semi-certified, because the proof certificate is built at run-time. At the present stage, our implementation is intended to be a testbed for experiments and further investigation on this reasoning paradigm. Section 6 gives some further information on our code.

2 A WORD ABOUT THE HOL LIGHT THEOREM PROVER

In the HOL system, there are two fundamental datatypes called term and theorem. Terms model fragments of (well-formed) mathematical expressions. Theorems are Boolean terms that are proved correct according to a fixed set of logical rules. Examples of both a term and a theorem in the concrete syntax of HOL Light are

```
2 + 2
```
and

```
|- 2 + 2 = 4.
```

Notice that terms are written enclosed in backquotes while theorems use the entailment symbol $\vdash$.

A theorem as $\vdash b$ is a first-class value composed by a list of terms as and a body b, for instance

```ml
# ARITH_SUC;;
val it : thm =
  |- (!n. SUC (NUMERAL n) = NUMERAL (SUC n)) /
     SUC _0 = BIT1 _0 /
     (!n. SUC (BIT0 n) = BIT1 n) /
     (!n. SUC (BIT1 n) = BIT0 (SUC n))
```

is synthetized via regular function call of prove that actually consumes the theorem's body and the corresponding proof.

```ml
let ARITH_SUC = prove
  (`(!n. SUC(NUMERAL n) = NUMERAL(SUC n)) /
   (SUC _0 = BIT1 _0) /
   (!n. SUC (BIT0 n) = BIT1 n) /
   (!n. SUC (BIT1 n) = BIT0 (SUC n))`,
    REWRITE_TAC[NUMERAL; BIT0; BIT1; DENUMERAL ADD_CLAUSES]);;
```

The Boolean connectives ‘∧’, ‘∨’, ‘⇒’ are represented in ASCII encoding ‘\and’, ‘\or’ and ‘\implies’, respectively. Universal and existential quantifier ‘∀x’. P x and ‘∃x. P x’. Other syntactic elements are borrowed from the ML world, such as the notation for concrete lists ‘[x1;...].’

As the name suggests, HOL (Higher-Order Logic) implements a higher-order language based on a variant of the typed lambda calculus. Hence, in a rough comparison with classical logic programming languages, our system is closer to $\lambda$Prolog [9] than the usual (first-order) Prolog.

Interactive proofs in HOL Light are performed by running tactics that operate on a context called goal, which represents the intermediate status of the current logical reasoning. There are simple tactics that model basic logical inference steps as well as sophisticated tactics that implement powerful decision procedures.

From the theorem proving perspective, our work consists of extending the HOL Light’s tactic mechanism by introducing specific ideas coming from the miniKanren methodology. The resulting system allows the user to build proof scripts either with tactics or solvers, and the resulting theorems will be available to the programming environment regardless of which proof mechanism has been utilized. In particular, the new theorems can be built on top of the standard library of HOL Light, populated by several thousand theorems.

3 A SIMPLE EXAMPLE

To give the flavor of our framework, we show an example of how to perform simple computations on lists. Let us consider the problem of computing the concatenation of two lists [1; 2] and [3]. One idiomatic way to
approach this problem in HOL is by using conversions [11]. Conversions are ML procedures that receive as input a term \( t \) and output a theorem of the form \( \vdash t = t' \). The term \( t' \) is the result of the computation, and the theorem itself is the certificate that guarantees its correctness. Let us show first how conversions are used before describing how one can perform the same task using our framework.

In HOL Light, one has the constant \( \text{APPEND} \) and the equational theorem (of the same name) that characterize it
\[
\vdash (\forall l. \text{APPEND } [] l = l) \land \\
(\forall h t l. \text{APPEND } (h :: t) l = h :: \text{APPEND } t l)
\]

We can then use the conversion \texttt{REWRITE_CONV} which performs the rewriting. The ML command is
\[
\texttt{# REWRITE_CONV [\text{APPEND}] `\text{APPEND } [1;2] [3]`;}
\]
which produces the theorem
\[
\vdash \text{APPEND } [1; 2] [3] = [1; 2; 3]
\]

Our implementation allows us to address the same problem from a logical point of view. We start by recalling two theorems that are proved – via list structural induction – during the bootstrap procedure of HOL Light, namely
\[
\texttt{# \text{APPEND_NIL};;}
\]
\[
\text{val it : thm = } \vdash \forall l. \text{APPEND } [] l = l
\]

and
\[
\texttt{# \text{APPEND_CONS};;}
\]
\[
\text{val it : thm = } \vdash \forall x xs ys zs. \text{APPEND } xs ys = zs \\
\quad \Rightarrow \text{APPEND } (x :: xs) ys = x :: zs
\]
to give the logical rules, in form of Horn clauses, that characterize the \text{APPEND} operator. Then we define a \texttt{solver}
\[
\texttt{let \text{APPEND_SLV} : solver =}
\]
\[
\texttt{REPEAT_SLV (CONCAT_SLV (ACCEPT_SLV \text{APPEND_NIL})} \\
\quad \texttt{(RULE_SLV \text{APPEND_CONS})});
\]
which implements the most obvious strategy for proving a relation of the form `\text{APPEND} x y = z` by structural analysis on the list `x`. The precise meaning of the above code will be clear later; however, this can be seen as the direct translation of the Prolog program

\[
\text{append([],X,X),}
\text{append([X|Xs],Ys,[X|Zs]) :- append(Xs,Ys,Zs).}
\]

Then, the problem of concatenating the two lists is described by the term
\[
`\exists x. \text{APPEND } [1;2] [3] = x`
\]
where the binder `\exists` is a syntactic variant of the usual existential quantifier `\exists`, which introduces the meta-variables of the query.

The following command
\[
\texttt{list_of_stream}
\]
\[
\texttt{(solve \text{APPEND_SLV}} \\
\quad `\exists x. \text{APPEND } [1; 2] [3] = x`);}
\]
runs the search process where (i) the solve function starts the proof search and produces a stream (i.e., a lazy list) of solutions and (ii) the outermost list_of_stream transforms the stream into a list.

The output of the previous command is a single solution which is represented by a pair where the first element is the instantiation for the meta-variable `x` and the second element is a HOL theorem
val it : (term list * thm) list = 
[(`\x = [1; 2; 3]`, |- APPEND [1; 2] [3] = [1; 2; 3])]

Since the theorem is the instantiation of the original query term, it certifies the correctness of the solution.

Now comes the interesting part: as in logic programs, our search strategy (i.e., the APPEND_SLV solver) can be used for backward reasoning. Consider the variation of the above problem where we want to enumerate all possible splits of the list [1; 2; 3]. This can be done by simply changing the goal term in the previous query:

```ml
# list_of_stream
   (solve APPEND_SLV
      `??x y. APPEND x y = [1;2;3]`);
```

val it : (term list * thm) list = 
[(`\x = []; \y = [1; 2; 3]`, |- APPEND [] [1; 2; 3] = [1; 2; 3]);
 (`\x = [1]; \y = [2; 3]`, |- APPEND [1] [2; 3] = [1; 2; 3]);
 (`\x = [1; 2]; \y = [3]`, |- APPEND [1; 2] [3] = [1; 2; 3]);
 (`\x = [1; 2; 3]; \y = []`, |- APPEND [1; 2; 3] [] = [1; 2; 3])]

The system finds the above solutions by filtering and refining a stream of substitutions, precisely in the same way it is done in any typical miniKanren implementation; eventually, the interesting part is the associated theorems that are synthesized.

4 A LIBRARY OF SOLVERS

Our framework is based on ML procedures called solvers which generalize classical HOL tactics in two ways: (i) they facilitate the manipulation of meta-variables (and their associated substitutions) in the goal\(^1\) and (ii) they allow the proof search to backtrack. Before digging into the description of what a solver is, we warn the reader that the word goal has a different meaning in miniKanren and HOL. For the former, a goal is a function that consumes a substitution and produces a stream of substitutions; for the latter, a goal is a pair of (already proved) assumptions and a term that still has to be proved. From now on, we will use the word goal in the sense of HOL.

For the sake of completeness, it is worth to describe the differences among goals, tactics, and solvers.

On the one hand, the refinements that a miniKanren goal does on substitutions are performed by a HOL tactic which takes a HOL goal apart into a tuple \((M, S, f)\), where \(M\) is a set collecting the introduced meta-variables so far, \(S\) is a list of (sub)goals, and \(f\) is a function that certifies the performed refinement. The usual HOL routine is to push and pop those tuples in a stack that represents the steps left to prove the claimed term – whenever the stack gets empty, the proof is completed.

On the other hand, a solver is a function that consumes a HOL goal as well as a tactic does, and produces a stream of such tuples that actually allows us to equip HOL Light with backtracking. To tie the knot, solvers extend tactics in the sense that every HOL tactic can be “promoted” into a solver using the ML function `TACTIC_SLV : tactic -> solver`.

We provide a library of basic solvers, usually having a name that ends in _SLV. For the rest of the paper, the following elementary solvers

\(^1\)The tactic mechanism currently implemented in HOL Light already provides basic support for meta-variables in goals. However, it seems to be used only internally in the implementation of the intuitionistic tautology prover `ITAUT_TAC`. 
• RULE_SLV : thm -> solver, that implements the backward chaining rule;
• ACCEPT_SLV : thm -> solver, that solves a goal by unifying with the supplied theorem;
• CONJ_SLV : solver, that splits a goal using the introduction rule of the conjunction;
• REFL_SLV : solver, that solves a goal which is an equation by unifying of the left- and right-hand sides;
• ALL_SLV : solver, that leaves the goal unmodified.

Please note that, as in miniKanren systems, the unification procedure employed is not hard-wired by our framework, and each solver can implement its own unification strategy. We see two main interesting variants that one would have at disposal. The first one is to use pattern matching instead of unification; this would allow for a mechanism of input/output modes as in certain Prolog implementations. The second one would be to use a higher-order unification algorithm to unleash the full expressivity of the underlying higher-order language.

Solvers are highly compositional, as tactics in HOL and goals in miniKanren are, and complex solvers can be built from simpler ones using high-order functions. For instance, given two solvers $s_1$ and $s_2$ the solver combinator CONCAT_SLV make a new solver that collect sequentially all solutions of $s_1$ followed by all solutions of $s_2$. This is the most basic construction for introducing backtracking into the proof strategy. The solver COLLECT_SLV iterates CONCAT_SLV over a list of solvers. Two other high-order solvers are (i) THEN_SLV : solver -> solver -> solver which combines sequentially two solvers and (ii) REPEAT_SLV : solver -> solver that keeps applying a given solver. Unlike Prolog, miniKanren uses a complete search strategy by default and that is provided in our system as well by the solver

\[
\text{let INTERLEAVE_SLV (slvl:solver list) : solver} = \\
\text{if slvl = [] then NO_SLV else} \\
\text{mergef_stream slvl []} ;;
\]

that relies on the stream combinator

mergef_stream : ('b -> 'a stream) list -> (unit -> 'a stream) list -> 'b -> 'a stream

which merges two lists of streams by interleaving each one of them.

Solvers (as for classical HOL tactics) can be used interactively by means of the following essential commands:
• gg (term) starts a new goal;
• ee (solver) applies a solver to the current goal state;
• bb () restores the previous goal state (i.e., undo the previous ee command);
• top_thms () returns the stream of solutions found.

Here is an example of interaction. We first introduce the goal, notice the use of the binder (??) for the metavariable $x$:

\[
\text{# gg `??x. 2 + 2 = x`;;}
\]

val it : mgoalstack = `2 + 2 = x`

Metavariabes: `x`,
one possible solution is by using reflexivity that closes the proof

\[
\text{# ee REFL_SLV;;}
\]

val it : mgoalstack = No sub(m)goals
and allows us to form the resulting theorem

\[
\text{# list_of_stream(top_thms());;}
\]

val it : (instantiation * thm) option list = [Some ((([], [(`2 + 2 = x`), ([], [])]), |- 2 + 2 = 2 + 2)]

Now, if one want to find a different solution, we can restore the initial state
# bb();
val it : mgoalstack = `2 + 2 = x`
Metavariables: `x`,
then use a different solver, for instance by unifying with the equational theorem |- 2 + 2 = 4, which can be automatically proved using the HOL procedure ARITH_RULE,

# ee (ACCEPT_SLV(ARITH_RULE `2 + 2 = 4`));;
val it : mgoalstack = No sub(m)goals

and, again, take the resulting theorem

# list_of_stream(top_thms());;
val it : (instantiation * thm) option list = [Some ((([], [`4`, `x=?, x`]), []), |- 2 + 2 = 4)]

Finally, we can change the proof strategy to find both solutions by using backtracking

# bb();
val it : mgoalstack = `2 + 2 = x`
Metavariables: `x`,

# ee (CONCAT_SLV REFL_SLV (ACCEPT_SLV(ARITH_RULE `2 + 2 = 4`)));
val it : mgoalstack = No sub(m)goals

# list_of_stream(top_thms());;
val it : (instantiation * thm) option list = [Some ((([], [`2 + 2`, `x=?`]), []), |- 2 + 2 = 2 + 2);
Some ((([], [`4`, `x=?`]), []), |- 2 + 2 = 4)]

The function solve : solver -> term -> (term list * thm) stream runs the proof search non interactively and produces a list of solutions as already shown in Section 3. In this last case it would be

# list_of_stream (solve (CONCAT_SLV REFL_SLV (ACCEPT_SLV(ARITH_RULE `2 + 2 = 4`))))
val it : ((term * term) list * thm) list = [[[(`2 + 2`, `x=?`)], |- 2 + 2 = 2 + 2); ([(`4`, `x=?`)], |- 2 + 2 = 4)]

5 CASE STUDY: EVALUATION FOR A LISP-LIKE LANGUAGE

The material in this section is strongly inspired by the ingenious work of Byrd, Holk, and Friedman about the miniKanren system [3], where the authors work with the semantics of the Scheme language. Here we target a dynamically scoped variant of the LISP language—not unlike it is done in [2]—formalized as an object language inside the HOL prover. The HOL prover could be a powerful tool for a formal study of the meta-theory of a programming language such as LISP. In this perspective, this section may have a scientific interest beyond the entertaining nature of the example it is going to present.

First, we need to extend our HOL Light environment with an object datatype sexp for encoding S-expressions according to the following BNF grammar

sexp ::= Symbol string
| List (sexp list)
For instance, the sexp `(list a (quote b))` is represented as HOL term with

```
`List [Symbol "list";
    Symbol "a";
    List [Symbol "quote";
    Symbol "b"]`
```

This syntactic representation can be hard to read and gets quickly cumbersome as the size of the terms grows. Hence, we also introduce a notation for concrete sexp terms, which is activated by the syntactic pattern `'(…)`.
For instance, the above example is written in the HOL concrete syntax for terms as
```
`'(list a (quote b))`
```
With this setup, we can easily specify the evaluation rules for our minimal LISP-like language. This is a ternary predicate `EVAL e x y` which satisfies the following clauses:

1. quoted expressions
   ```
   # EVAL_QUOTED;;
   |- !e q. EVAL e (List [Symbol "quote"; q]) q
   ```
2. variables
   ```
   # EVAL_SYMB;;
   |- !e a x. RELASSOC a e x ==> EVAL e (Symbol a) x
   ```
3. lambda abstractions
   ```
   # EVAL_LAMBDA;;
   |- !e l. EVAL e (List (CONS (Symbol "lambda") l))
       (List (CONS (Symbol "lambda") l))
   ```
4. lists
   ```
   # EVAL_LIST;;
   |- !e l l'. ALL2 (EVAL e) l l'
       ==> EVAL e (List (CONS (Symbol "list") l)) (List l')
   ```
5. unary applications
   ```
   # EVAL_APP;;
   |- !e f x' v b y.
       EVAL e f (List [Symbol "lambda"; List[Symbol v]; b]) /\
       EVAL e x' /\ EVAL (CONS (x',v) e) b y
       ==> EVAL e (List [f; x]) y
   ```
The predicate `EVAL` is inductively defined, i.e., it is (informally) the smallest predicate that satisfies the above rules.

We now use our framework for running a certified evaluation process for this language. First, we define a solver for a single step of computation

```
let STEP_SLV : solver =
  COLLECT_SLV
  [CONJ_SLV;
   ACCEPT_SLV EVAL_QUOTED;
   THEN_SLV (RULE_SLV EVAL_SYMB) RELASSOC_SLV;
   ACCEPT_SLV EVAL_LAMBDA;
   RULE_SLV EVAL_LIST;
   RULE_SLV EVAL_APP;
```
In the above code, we collect the solutions of several different solvers. Other than the five rules of the EVAL predicate, we include specific solvers for conjunctions and the two predicates REL_ASSOC and ALL2.

Let us mention that the definition of solvers such us STEP_SLV above could be automatically derived from the set of clauses by performing a syntactical analysis. However, we did not invest time so far on this kind of improvements, since we are still experimenting with the basis of the system.

The top-level recursive solver for the whole evaluation predicate is now easy to define:

```ml
let rec EVAL_SLV : solver =
  fun g -> CONCAT_SLV ALL_SLV (THEN_SLV STEP_SLV EVAL_SLV) g;;
```

Let us make a simple test. The evaluation of the expression

```ml
((lambda (x) (list x x x)) (list))
```

can be obtained as follows:

```ml
# get (solve EVAL_SLV
`??ret. EVAL []
'>((lambda (x) (list x x x)) (list))
`ret`);
```

val it : term list * thm =

```
(
`ret = `(() () ()`

`|- EVAL [] `((lambda (x) (list x x x)) (list)) `((() () ())))
```

Again, we can use the declarative nature of logic programs to run the computation backwards. For instance, one intriguing exercise is the generation of quine programs, that is, programs that evaluate to themselves. In our formalization, they are those terms \( q \) satisfying the relation \( \text{EVAL} [] q q \). The following command computes the first two quines found by our solver.

```ml
# let sols = solve EVAL_SLV `??q. EVAL [] q q`;;
# take 2 sols;;
```

val it : (term list * thm) list =

```
([`
`q = List (Symbol "lambda" :: _3149670)`

`|- EVAL [] (List (Symbol "lambda" :: _3149670))
(List (Symbol "lambda" :: _3149670)));
```

```
([`
`q =
List
(List
[Symbol "lambda": List [Symbol _3220800];
 List [Symbol "list": Symbol _3220800; Symbol _3220800]];
List
[Symbol "lambda": List [Symbol _3220800];
 List [Symbol "list": Symbol _3220800; Symbol _3220800]]
`|- EVAL []
(List
[List
[Symbol "lambda": List [Symbol _3220800];
 List [Symbol "list": Symbol _3220800; Symbol _3220800]]
`|- EVAL []
(List
[List
[Symbol "lambda": List [Symbol _3220800];
 List [Symbol "list": Symbol _3220800; Symbol _3220800]]
```
One can easily observe that any lambda expression is trivially a quine for our language. This is indeed the first solution found by our search:

```
q = List (Symbol "lambda" :: _3149670)
```

The second solution is more interesting. Unfortunately, it is presented in a form that is hard to decipher. A simple trick can help us to present this term as a concrete sexp term: it is enough to replace the HOL generated variable `_3149670` with a concrete string. This can be done by an ad-hoc substitution:

```
# let [_; i2,s2] = take 2 sols;;
# vsubst ["x",hd (frees (rand (hd i2)))] (hd i2);;
```

If we take one more solution from `sols` stream, we get a new quine which, interestingly enough, is precisely the one obtained in [3]:

```
q = '((quote (lambda (x) (list x (list (quote quote) x))))
    (quote (quote (lambda (x) (list x (list (quote quote) x))))))
```

6 DESCRIPTION OF OUR CODE

The HOL Light theorem prover and our extension are written in OCaml and, more precisely, in a rather minimal and conservative subdialect of it, which should be understandable to everyone that has some familiarity with any of the languages of the ML family. Our code is available from a public repository, in particular, a release has been created at https://github.com/massimo-nocentini/kanren-light/releases/tag/miniKanren2020.

Besides the code presented in this article, the above repository contains some other experiments of various nature, including the following:

- An implementation of the Quicksort algorithm. The procedure outputs the sorted list together with a formal proof that such list is indeed sorted and in bijection with the input lists.
- A solver for the Monte Carlo Lock, a brain teaser by Smullyan [13], where one has to unlock a safe whose key is the fixed point of an abstract machine. The interesting thing is that the solver is essentially derived from the formal specification in HOL of the puzzle.
• An intuitionistic first-order tautology prover ITAUT_SLV. This is inspired by a similar tactic ITAUT_TAC already available in HOL Light. However, HOL tactics cannot backtrack, which implies that ITAUT_TAC is incomplete. Our solver ITAUT_SLV is coded in pretty much the same way as ITAUT_TAC, but it is complete (although this latter fact can be claimed only via a meta-theoretical analysis).

With respect to the existing framework of HOL Light, our effort didn’t apply any change to both existing structures and computation flow, it just adds a parallel way of proving things. The connection point is the type \texttt{mgoal = term list * goal} that enhances a goal with a list of meta-variables and, eventually, all the complexity of the presented work lies in their correct bookkeeping and in the handling of goal streams.

Our code is conceived for experimenting, and very little or no attention has been paid to optimizations. Despite this, the OCaml runtime and the HOL Light implementation have an established reputation of being time- and memory-efficient systems (compared with similar tools). From our informal tests, it seems that this efficiency is, at least partially, inherited by our implementation.

7 FUTURE AND RELATED WORK

We presented a rudimentary framework inspired by miniKanren systems implemented on top of the HOL Light theorem prover that enables a logic programming paradigm for proof searching. More specifically, it facilitates the use of meta-variables in HOL goals and permits backtracking during the proof construction. Despite the simplicity of the present implementation, we have already shown the implementation of some paradigmatic examples of logic-oriented proof strategies.

It would be interesting to enhance our framework with more features:

• Implement higher-order unification as Miller’s higher-order patterns, so that our system can enable higher-order logic programming in the style of \texttt{\lambda}Prolog [4].

• Support constraint logic programming [8], e.g., by adapting the data structure that represents goals.

Besides extending our system with new features, we plan to test it on further examples. One natural domain of applications would be the development of decision procedures. While HOL Light already offers some remarkable tools for automatic theorem proving, our system could offer new alternatives leaning to simplicity and compositionality. For instance, we could try to translate in our system the approach of \texttt{\alpha}lean TAP [10] for implementing an automatic procedure for first-order classical logic in HOL Light analogous to the \texttt{blast} tactic of Paulson [12] in Isabelle.

REFERENCES


\footnote{The tactic \texttt{ITAUT_TAC} has a peculiar role in the HOL system. It is used during the bootstrap of the system to prove several basic logical lemmas. After the initial stages, a much more powerful and faster procedure for (classical) first-order logic \texttt{MESON_TAC} is installed in the system, and the \texttt{ITAUT_TAC} becomes superfluous.}